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# Theoretical Investigation on Inclusion Complex of (s)-2-Isopropyl-1-(o-nitrophenyl) Sulfonyl) Aziridine with $\boldsymbol{\beta}$-Cyclodextrin 

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The present work aims to study the theoretical chemistry applied to organic systems such as host/guest inclusion complexes. In literature, different molecular modeling computational methods have been used to study the complexation of the host $\beta$-cyclodextrin molecule ( $\beta$-CD) with the guest (S)-2-Isopropyl-1-(o-nitrophenyl) sulfonyl) aziridine molecule (AZ). Among such methods are semiempirical (PM3) and Density Functional Theory (DFT) calculations in gas and aqueous phases. The present paper focuses on complexation, interaction, deformation energies determination, besides geometries, electronic structure, and chemical reactivity to describe the changes of AZ during encapsulation in two phases and at two orientations. Long-range corrected hybrid functional (WB97X-D/6-31G (d) basis) was used and the results clearly indicate that the formed complex is energetically preferred in both phases. The orientation in which the guest molecule pointed toward the secondary hydroxyls of $\beta$-CD showed good compatibility with the experimental results. The Natural Population Analysis (NPA) charges obtained from NBO analysis were used in order to find out the possible coordination modes of the AZ compound with $\beta$-CD. Natural bond orbital analysis (NBO) and Non-covalent interaction (NCI) analysis were performed on the $\beta$ $\mathrm{CD} / \mathrm{AZ}$ complex to understand the different interactions. The 1 H nuclear magnetic resonance (NMR) of the complex was studied using the Gauge-Including Atomic Orbital (GIAO).

Keywords: $\beta$-Cyclodextrin, AZ, DFT, NBO and NCI

## INTRODUCTION

Cyclodextrins (CDs) are cyclic oligosaccharides that can be obtained artificially by enzymatic conversion of amylose using the enzyme cyclodextrin glycosyltransferase (CGTase) of bacterial origin. The three most commonly used CDs are $\alpha-\mathrm{CD}, \beta-\mathrm{CD}$, and $\gamma-\mathrm{CD}$, which consist of 6,7 , and 8 subunits of D-glucopyranose, respectively [1,2] linked together by $\alpha$-glycosidic bonds ( $1 \rightarrow 4$ ). Thus the cavity formed has non-polar carbonate and hydrophobic environment, while the outer part contains many hydroxyls

[^0]groups, which leads to the solubility of cyclodextrins in an aqueous medium. Due to the presence of mentioned nonpolar cavity, cyclodextrins are able to form inclusion complexes in an aqueous medium with a variety of hydrophobic host molecules; the formation of complex depends on a proper match between the size of the host molecule and the cyclodextrin molecule. In this article, $\beta$ CD (Fig. 1a) has been used as a host due to its non-toxicity to the human organism. It has been used frequently in the food, pharmaceutical, and cosmetic industries.

Aziridine is an interesting class due to its chemical reactivity. They are valuable natural and/or synthetic organic compounds that are widely used to access many


Fig. 1. Molecular structures and atom numbering for $\beta-C D$ (a) and $A Z$ (b).
medicines and bioactive products [3,4].
Molecular modeling is a technique that not only can represent the chemical properties and chemical reactions, but also to manipulate the structure of model compounds in two or three dimensions. Actually, there are a large number of theoretical methods used in the molecular modeling of supramolecular systems. Among these methods are molecular mechanics (MM), molecular dynamics (MD), semi-empirical methods, and DFT methods that are widely used for large systems to determine the graphical representation of the geometry or configuration of the atoms of a molecule and assessing the physical and chemical properties of the molecule. Molecular modeling associated to a graphical representation of the stereochemistry allows interpretation of physical and chemical phenomenon, suggesting new experiments, and thus analyzing the results in a more significant way than the traditionally used experiments. In fact, both approaches, pure theoretical and experiment, are complementary.

This work is composed of two parts: in the first part, the processes of AZ inclusion in the $\beta-C D$ cavity are examined using the semi-empirical PM3 method for determining minimum energy structures. In the second part, the more
stable complex, obtained through PM3 calculations, are improved by the density functional theory (DFT) using the functionals B3LYP [5,6], WB97X-D [7], and B97D3 [8,9], and $6-31 \mathrm{G}(\mathrm{d})$ basis set in gas and aqueous phases. In this part, complexation, interaction, and deformation energies, geometries, thermodynamic parameters, frontier molecular orbitals, the global indices of reactivity, the (NPA) atomic charges, and natural bond orbital (NBO) are calculated. We also systematically compare the chemical shifts deviations obtained from Gauge-Including Atomic Orbital calculations (GIAO) and corresponding experimental values of 1H NMR [10].

Finally, analysis of non-covalent interactions (NCI) as a robust approach for evaluating intermolecular interactions is considered.

## COMPUTATIONAL DETAILS

Quantum mechanical calculations were performed using density functional theory (DFT) applying the functionals B3LYP [5,6], WB97X-D [7], and B97D3 [8,9], and the 6$31 \mathrm{G}(\mathrm{d})$ basis set in the gas and aqueous phases. Gaussian 09 [11] and MOPAC 2016 [12] software were used.


Fig. 2. Coordinate systems used to define the complexation process for both orientations.

The initial structures of the guest $A Z$ and the host $\beta-C D$ were retrieved from PUBCHEM compound database [13] and Chem office3D Ultra (version10, Cambridge Software) [14], respectively The AZ/ $\beta$-CD complex was generated by Hyperchem 7.5 [15] molecular modeling software. The AZ and $\beta$-CD structures were optimized by the semi-empirical PM3 method [16]. Semi-empirical calculations were first performed using MOPAC 2016 [12], and the visualization and treatment of results were done using Gauss view 5.0 [17]. The optimized host and guest structures are shown in Fig. 1.

The coordinate system used to define complexation process is shown in Fig. 2. To inclusion the guest AZ molecule inside the $\beta-C D$, methods described in the literature have been followed [18-22]. The $\beta$-CD host is positioned at the XY plane and its center is defined as the origin of the systems coordinates. The secondary hydroxyl groups of $\beta$-CD are oriented in the positive direction of the $Z$ axis, and then the mass center of the guest molecule $A Z$ is placed at the XYZ reference center. The center of the $\beta-C D$ host is located at the origin of the reference frame, $\mathrm{O}(0$, $0.0)$ and $\beta-C D$ is in fixed position. The guest to host is then moved along the Z axis from -5 to +5 A 0 with $1 \AA$ step. Figure 2 shows two directions for insertion of guest molecule into the $\beta$-CD host molecule. This allows us to see the effects of the two types of hydroxyls: Orientation A, in which the aromatic ring is oriented toward the secondary hydroxyls of $\beta-C D$, and Orientation $B$, in which the
aromatic ring is oriented towards the basic hydroxyls of $\beta$-CD.

To define the host-guest interaction in the optimized geometries, several energetic expressions were used: complexation energy [23], interaction energy [24,25], and deformation energy [26].

The complexation energy is defined as the difference between the energy of the complex and the energy of the individual components in their optimized geometries, Eq. (1).

$$
\begin{equation*}
\Delta \mathrm{E}_{\text {complexation }}=\mathrm{E}_{\text {complex }}-\left[\mathrm{E}_{\beta \text {-CDfree }}+\mathrm{E}_{\mathrm{AZ} \text { free }}\right] \tag{1}
\end{equation*}
$$

Where $\mathrm{E}_{\text {complex }}$ represents the energy of the complex, $\mathrm{E}_{\beta-\mathrm{CD}}$ represents the energy of $\beta-C D$ before the complexation, and $\mathrm{E}_{\mathrm{AZ}}$ represents the energy of the AZ guest molecule before the complexation.

Interaction energy represents the interaction between the host molecule and the guest molecule in the inclusion complex (Eq. (2)).

$$
\begin{equation*}
\Delta \mathrm{E}_{\text {interaction }}=\mathrm{E}_{\text {complex }}-\left[\mathrm{E}_{\beta-\mathrm{CDsp}}+\mathrm{E}_{\mathrm{AZsp}}\right] \tag{2}
\end{equation*}
$$

Where $\mathrm{E}_{\text {complex }}$ represents the energy of the complex, $\mathrm{E}_{\beta-\mathrm{CD}}$ represents the energy of $\beta-C D$ after the complexation, and $\mathrm{E}_{\mathrm{AZ}}$ represents the energy of the guest molecule after the complexation.

The last energy is the deformation energy of each host


Fig. 3. Complexation energies of the inclusion of $A Z$ into $\beta$ CD optimized at different positions Z using (PM3 calculations).
and guest component during the formation of the complex. It is defined as the difference between the energy of the fully optimized component compared to its energy in the complex (Eqs. (3) and (4)).

$$
\begin{align*}
& \mathrm{E}_{\text {deformation }}(\beta-\mathrm{CD})=\mathrm{E}_{\beta-\mathrm{CD} \text { sp }}-\mathrm{E}_{\beta-\mathrm{CD} \text { free }}  \tag{3}\\
& \mathrm{E}_{\text {deformation }}(\mathrm{AZ})=\mathrm{E}_{\mathrm{AZ} \text { sp }}-\mathrm{E}_{\mathrm{AZ} \text { free }} \tag{4}
\end{align*}
$$

## RESULTS AND DISCUSSIONS

## Energies

The graphical presentation of the energy changes for the insertion of AZ in the $\beta-\mathrm{CD}$ are shown as two curves in Fig. 3. From these curves, it is observed that the minimum energy of the more stable structures falls at $Z=-3 \AA$, and $Z=-3 \AA$ for the two orientations A and B, respectively. The corresponding complexation energies are: $-16.260 \mathrm{kcal} \mathrm{mol}^{-}$ ${ }^{1}$ and $-17.063 \mathrm{kcal} \mathrm{mol}^{-1}$ for orientations A and B , respectively. After that, the resulting complex was optimized at a high computational level using the following functionals: B3LYP/6-31G(d) and WB97X- D/6-31G(d) and B97D3/6-31G(d)) in gas and aqueous phases. The calculation of the different energy conditions for the two orientations were reported and compared in Table 1. From Table 1, it is observed that, in contrast to PM3 semiempirical calculations, the interaction energy is in favor of

Table 1. The Different Energies of $\beta-C D / A Z$ in the Gas and Aqueous Phase were Calculated by Methods: B3LYP/6-31G(d), WB97X-D/6-31G(d), and B97D3/6-31G(d)

|  | Gas phase |  | Aqueous phase |  |
| :--- | :---: | :---: | :---: | :---: |
|  | Orientation A | Orientation B | Orientation A | Orientation B |
| $\mathrm{B} 3 \mathrm{LYP} / 6-31 \mathrm{G}(\mathrm{d})$ |  |  |  |  |
| $\Delta \mathrm{E}_{\text {complexation }}$ | -19.60 | -6.80 | -11.37 | -3.52 |
| $\Delta \mathrm{E}_{\text {interaction }}$ | $-25.58(-12.01)$ | $-8.74(0.31)$ | -14.82 | -4.42 |
| $\mathrm{E}_{\mathrm{DEF}(\text { Host }}$ | 9.52 | 1.38 | 5.79 | 0.53 |
| $\mathrm{E}_{\mathrm{DEF} \text { (Guest) }}$ | -3.54 | 0.56 | -2.34 | 0.36 |
| $\mathrm{WB} 97 \mathrm{X}-\mathrm{D} / 6-31 \mathrm{G}(\mathrm{d})$ |  |  |  |  |
| $\Delta \mathrm{E}_{\text {complexation }}$ | -41.06 | -37.02 | -31.85 | -31.38 |
| $\Delta \mathrm{E}_{\text {interaction }}$ | $-52.35(-39.24)$ | $-46.56(-32.00)$ | -40.37 | -38.67 |
| $\mathrm{E}_{\mathrm{DEF}(\text { Host }}$ | 12.84 | 6.74 | 9.05 | 4.53 |
| $\mathrm{E}_{\mathrm{DEF}(\text { Guest })}$ | -1.53 | 2.80 | -0.52 | 2.75 |
| $\mathrm{~B} 97 \mathrm{D} 3 / 6-31 \mathrm{G}(\mathrm{d})$ |  |  |  |  |
| $\Delta \mathrm{E}_{\text {complexation }}$ | -41.66 | -37.85 | -33.41 | -33.89 |
| $\Delta \mathrm{E}_{\text {interaction }}$ | $-52.15(-36.65)$ | $-47.22(-30.38)$ | -40.86 | -39.77 |
| $\mathrm{E}_{\mathrm{DEF} \text { (Host) }}$ | 12.20 | 6.66 | 8.17 | 3.77 |
| $\mathrm{E}_{\mathrm{DEF} \text { (Guest) }}$ | -1.70 | 2.70 | -0.71 | 2.10 |



Fig. 4. Geometrical structures of the most stable complexes obtained from B3LYP/6-31G(d) (a, b), WB97X-D/6$31 \mathrm{G}(\mathrm{d})\left(\mathrm{a}^{\prime}, \mathrm{b}^{\prime}\right)$ and B97D3/6-31G(d) (a", $\left.\mathrm{b}^{\prime \prime}\right)$ calculations for AZ/ $\beta$-CD in gas phase.


Fig. 5. Geometric structures of the free $\beta-C D(a)$ and the $A Z / \beta-C D$ complex $(b, c)$ in the orientations $A$ and $B$ calculated by the method WB97X-D/6-31G(d) in the gas phase.
orientation A. It is worth noting that the complexation and interaction energies have negative values, indicating that the inclusion of $A Z$ in $\beta-C D$ is thermodynamically favorable, and the encapsulation processes and the calculations are in good agreement with experimental data [10]. Significantly higher values of $\Delta \mathrm{E}_{\text {interaction }}$ energy obtained using WB97X$\mathrm{D} / 6-31 \mathrm{G}(\mathrm{d})\left(-52.35 \mathrm{kcal}_{\mathrm{mol}}{ }^{-1}\right)$ and $\mathrm{B} 97 \mathrm{D} 3 / 6-31 \mathrm{G}(\mathrm{d})$ $\left(-40.86 \mathrm{kcal} \mathrm{mol}^{-1}\right)$ methods, compared to B3LYP/6-31G(d) $\left(-25.58 \mathrm{kcal} \mathrm{mol}^{-1}\right)$ method. For the two methods, WB97X$\mathrm{D} / 6-31 \mathrm{G}(\mathrm{d})$ and B97D3/6-31G(d), the dispersion effect is an important factor to study the supramolecular systems; weak dispersion forces increase with increasing the number of atoms and the molecular weight [19]. The effects of electron correlation play an important role on the nature of intermolecular interaction probably having a considerable contribution to dispersion forces [19]. The solvent effect is indicated by energy difference between the gas and aqueous phases. The results of the deformation energies of the gas and aqueous phases calculated by the three functionals are shown in Table 1. From the results, the deformation energy of the $\beta-C D$ molecule is always higher than that of the $A Z$ molecule in both orientations, A and B . This confirms that the flexibility of the $\beta-C D$ structure plays an important role in increasing the intermolecular interaction and affects the stability of the whole system upon complexation [25]. Especially, the primary hydroxyl groups of $\beta-C D$ play an important role in the formation of bonds with $A Z$
(see Fig. 5).
We also note that the deformation energy of the $\beta-C D$ molecule calculated by the classic B3LYP method ( $9.52 \mathrm{kcal} \mathrm{mol}^{-1}$ ) is lower than that obtained using the WB97X-D/6-31G(d) ( $12.84 \mathrm{kcal} \mathrm{mol}{ }^{-1}$ ) and B97D3/6$31 \mathrm{G}(\mathrm{d})\left(12.20 \mathrm{kcal} \mathrm{mol}^{-1}\right)$ methods. This indicates that WB97X-D/6-31G(d) and B97D3/6-31G(d) predict better optimized geometries than the traditional B3LYP method.

To improve the accuracy of our theoretical results, from the computation of optimized geometries, the interaction energy was corrected considering the basic set superposition error (BSSE) [27] using the counterpoise method [28] through (Eq. (5)).

$$
\begin{equation*}
\Delta \mathrm{E}_{\text {interaction }}=\mathrm{E}_{\text {complex }}-\left[\mathrm{E}_{\beta-\mathrm{CDsp}}+\mathrm{E}_{\mathrm{Azsp}}\right]+\mathrm{BSSE} \tag{5}
\end{equation*}
$$

BSSE corrected energies are shown in brackets in Table 1.

## Geometry Optimization

According to our results, most of the geometric parameters have approximately the same values in both the gas state and the aqueous state. This let us to provide a single interpretation in the gas axis. Tables 2 and 3 report the geometrical parameters (bond lengths, bond angles, and dihedral angles) of the AZ and $\beta$-CD molecules before and after complexation, which are related to the most stable

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Table 2. Geometric Parameters (Bond Lengths, Bond Angles and Dihedral Angles) for AZ before and after Inclusion in $\beta$-CD Calculated with B3LYP/6-31G(d)/WB97X-D/6-31G(d)/B97D3/6-31G(d) in the Gas Phase

|  |  |  |  |
| :--- | :---: | :---: | :---: |
|  | AZ free | Gas phase |  |
| Bond lengths $(\AA)$ |  | Orientation A | Orientation B |
| O 164-O 161 | $2.54 / 2.52 / 2.56$ | $2.52 / 2.49 / 2.53$ | $2.53 / 2.51 / 2.54$ |
| O 164-S 162 | $1.45 / 1.44 / 1.46$ | $1.47 / 1.45 / 1.47$ | $1.45 / 1.44 / 1.46$ |
| S 162-O 161 | $1.46 / 1.45 / 1.47$ | $1.47 / 1.45 / 1.48$ | $1.47 / 1.45 / 1.47$ |
| N 163-C 165 | $1.45 / 1.45 / 1.46$ | $1.48 / 1.47 / 1.48$ | $1.46 / 1.45 / 1.47$ |
| Bond angles ( ${ }^{\circ}$ ) |  |  |  |
| S 162-O 164-C 151 | $42.10 / 41.96 / 41.92$ | $38.89 / 38.00 / 37.84$ | $42.04 / 42.35 / 42.02$ |
| S 162-O 164-O 161 | $29.75 / 29.49 / 29.39$ | $31.01 / 31.28 / 31.04$ | $30.32 / 30.23 / 30.24$ |
| S 162-N 163-O 164 | $33.20 / 33.32 / 33.54$ | $33.15 / 33.34 / 33.50$ | $33.18 / 33.22 / 33.43$ |
| S 162-N 163-O 161 | $34.01 / 34.20 / 33.87$ | $30.83 / 30.68 / 30.16$ | $33.24 / 33.16 / 32.53$ |
|  |  |  |  |
| N 158-O 159-O 160 | $27.31 / 27.18 / 27.00$ | $27.39 / 27.26 / 27.07$ | $27.33 / 27.44 / 27.34$ |
| Dihedral angles ${ }^{\text {(o) }}$ |  |  |  |
| S 162-O 164-O 161-C 151 | $-41.76 /-41.48 /-41.14$ | $-37.48 /-36.13 /-35.81$ | $-41.61 /-41.63 /-41.15$ |
| S 162-O 164-O 161-N 163 | $38.81 / 38.50 / 39.41$ | $32.49 / 32.32 / 32.13$ | $37.82 / 36.89 / 37.30$ |
| S 162-N 163-O 164-O 161 | $29.42 / 29.12 / 29.08$ | $26.27 / 26.35 / 25.65$ | $29.16 / 28.66 / 28.37$ |
| S 162-N 163-O 161-C 151 | $39.31 / 39.86 / 39.14$ | $46.47 / 47.45 / 47.97$ | $39.45 / 39.85 / 39.74$ |
| N 158-O 159-O 160-C 152 | $-2.04 /-2.42 /-2.46$ | $2.37 / 2.57 / 2.76$ | $-2.09 /-1.40 /-1.40$ |

Table 3. The Selected Parameters for Free $\beta$-CD and In-complex Forms Calculated with B3LYP/6-31G(d)/WB97X-D/6-31G(d)/B97D3/6-31G(d) Methods in the Gas Phase

|  | Gas phase <br> Orientation A |  |  |
| :--- | :---: | :---: | :---: |
| Primary hydroxyls |  |  | Orientation B |
| O 33-O 44 | $2.90 / 2.83 / 2.85$ | $4.37 / 4.21 / 4.32$ | $2.91 / 2.85 / 2.92$ |
| O 44-O 55 | $2.91 / 2.84 / 2.86$ | $4.48 / 4.16 / 4.26$ | $2.94 / 2.92 / 3.09$ |
| O 55-O 66 | $6.64 / 6.45 / 6.52$ | $6.56 / 6.21 / 6.30$ | $6.74 / 6.71 / 6.91$ |
| O 66-O 77 | $3.00 / 2.94 / 2.96$ | $3.25 / 3.22 / 3.16$ | $3.00 / 2.91 / 2.97$ |
| Secondary hydroxyls |  |  |  |
| O 71-O 60 | $5.61 / 5.60 / 5.63$ | $5.56 / 5.54 / 5.60$ | $5.68 / 5.66 / 5.69$ |
| O 60-O 49 | $5.27 / 5.22 / 5.23$ | $5.31 / 5.36 / 5.36$ | $5.27 / 5.23 / 5.20$ |
| O 49-O 38 | $5.50 / 5.44 / 5.49$ | $5.18 / 5.22 / 5.19$ | $5.51 / 5.37 / 5.35$ |
| O 38-O 27 | $5.65 / 5.57 / 5.65$ | $5.32 / 5.29 / 5.31$ | $5.61 / 5.37 / 5.53$ |

structures obtained with B3LYP/6-317G(d), WB97X-D/6$31 \mathrm{G}(\mathrm{d})$, and $\mathrm{B} 97 \mathrm{D} 3 / 6-31 \mathrm{G}(\mathrm{d})$ methods. As shown in Table 2, the results for the orientation A indicate that the initial geometry of guest AZ is completely changed. This is while the difference in the geometric parameters before and after the complexation slightly changed for the orientation B. Initially, there was a slight change observed in the bond lengths of the AZ before (O 164-S 162: 1.45/1.44/1.46 $\AA$ ) and after the complexation in the orientation A (O 164S 162: 1.47/1.45/1.47 $\AA$ ) and in the orientation B (O 164S 162: $1.45 / 1.44 / 1.46 \AA$ ). The real change was observed through the difference between the bond angles and dihedral angles of the $A Z$ molecule before and after the complexation. For orientation A, the difference between the S 162-O 164-O $161-\mathrm{N} 163$ dihedral angle (38.810/38.50\% $39.41^{\circ}$ ) of the free AZ molecule and the dihedral angle S 162-O $\left.164-\mathrm{O} 161-\mathrm{N} 163\left(32.49^{\circ} / 32.32^{\circ}\right) / 32.13^{\circ}\right)$ of AZ in the complex is important. The mentioned difference is more obvious compared to the similar results of dihedral angle S 162-O 164-O 161-N 163 (37.820/36.890/37.30 $)$ in the orientation $B$. This means that the guest $A Z$ in the orientation A must be profiled to fit the host $\beta-C D$ cavity and form a more stable inclusion complex. This result was confirmed by deformation energies (see Table 1). On the other hand, the distances between the primary and secondary hydroxyls' oxygens of $\beta-C D$ and AZ, before and after complexation, (Table 3) show significant distortion in the $\beta$-CD lumen compared to its initial geometry (see Fig. 5). In the orientation A, the O 33-O $44(2.83 \AA)$ and O 44-O $55(2.84 \AA)$ distances became longer $(4.21 \AA$ and $4.16 \AA$, respectively), which is due to interactions between O164 and H 117 from oxygen O44 and between O 159 and H 107 oxygen O 33 ; the latter is present in the orientation A, but not in the orientation B (see Fig. 5). This explains why the interaction energy of inclusion in the orientation A $\left(-52.35 \mathrm{kcal} \mathrm{mol}^{-1}\right)$ is less than that in the orientation B ( $-46.56 \mathrm{kcal} \mathrm{mol}^{-1}$ ) in both phases using all three functionals.

## Thermodynamic Properties

Calculations of standard thermodynamic parameters were performed using harmonic vibrational analysis [29]. Calculations were performed in vacuum and water at 1 atm pressure and temperature of 298.15 K using WB97X-D/6-

31G(d), and B97D3/6-31G(d) methods. The thermodynamic quantities of the $A Z / \beta-C D$ complex, such as the enthalpy change $\left(\Delta H^{\circ}\right)$, the thermal Gibbs free energy ( $\Delta \mathrm{G}^{\circ}$ ), and entropy contribution $\left(\Delta \mathrm{S}^{\circ}\right)$ are summarized in Table 4.

It was observed that the enthalpy values $\left(\Delta \mathrm{H}^{\circ}\right)$ are negative in both orientations, and these differences indicate that the inclusion process is enthalpically favorable. On the other hand, the enthalpy differences of the orientation A $\left(\Delta \mathrm{H}^{\circ}=-48.67 \mathrm{kcal} \mathrm{mol}^{-1}\right)$ were more negative than that in orientation $\mathrm{B}\left(\Delta \mathrm{H}^{\circ}=-42.89 \mathrm{kcal} \mathrm{mol}^{-1}\right)$, which is attributed to stronger van der Waals interactions [25] between $A Z$ and $\beta-C D$ in deeper penetration of the guest molecule into the hydrophobic host. Values of $\Delta \mathrm{G}^{\circ}=-60.01 \mathrm{cal} \mathrm{mol}^{-1} \mathrm{~K}^{-1}$ are negative and this indicates that the process of AZ inclusion in $\beta$-CD is spontaneous at 1 atm and 298.15 K . when the system is well arranged, the results of our theoretical calculations $\Delta \mathrm{G}^{\circ}<0$ is in good agreements with the data in the literature [10]. We can also see that the entropy $\left(\Delta \mathrm{S}^{\circ}\right)$ has a negative change in both orientations. This indicates that the formation of the complex is an exothermic process resulting from enthalpy [20]. Due to steric barrier, the negative change of the entropy $\left(\Delta \mathrm{S}^{\circ}\right)$ caused by molecular geometrical shape that limits the free shift of $\beta-C D$ cavity and rotation of AZ molecule [20].

## Frontier Molecular Orbitals (FMOs)

The occupied HOMO and unoccupied LUMO frontier molecular orbitals [30] play an important role in understanding the effect of guest molecule encapsulation within the host. HOMO is the electron donor and LUMO is the electron acceptor [31,32]. Results for the energies of HOMO and LUMO, and $\triangle \mathrm{E}$ (HOMO-LUMO) obtained by WB97X-D/6-31G(d) and B97D3/6-31G(d) methods in the gas and aqueous phases are shown in Table 4. The energy gap $\triangle \mathrm{E}$ (HOMO-LUMO) is an important measure of stability. The higher chemical values of $\triangle \mathrm{E}$ (HOMOLUMO) indicate higher stability and lower reactivity [3335]. The values of $\triangle \mathrm{E}$ (HOMO-LUMO) obtained by the two methods in the gas and aqueous phases of the $A Z / \beta-C D$ complex are -0.291 eV for orientation A and -0.297 eV for orientation B . This means that orientation A is more stable than orientation B. These results are in good agreement with the complexation energy results of the orientation A $\left(41.66 \mathrm{kcal} \mathrm{mol}^{-1}\right)$ and the orientation

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Table 4. Thermodynamic Parameters, HOMO, LUMO, $\triangle$ (HOMO-LUMO) and Global Descriptions of the AZ, $\beta-C D$, and AZ/ $\beta-C D$ Complex Computed by Methods WB97X-D/6-31G(d)/ B97D3/6-31G(d)) in the Gas and Aqueous Phases

| Gas phase |  |  |  |  |
| :--- | :---: | :---: | :---: | :---: |
|  | $\beta$-CD free | AZ free | Orientation A | Orientation B |
| $\Delta \mathrm{H}^{\circ}\left(\mathrm{kcal} \mathrm{mol}^{-1}\right)$ | - | - | $-48.67 /-48.35$ | $-42.89 /-44.71$ |
| $\Delta \mathrm{G}^{\circ}\left(\mathrm{kcal} \mathrm{mol}^{-1}\right)$ | - | - | $-30.70 /-32.97$ | $-24.80 /-26.43$ |
| $\Delta \mathrm{~S}^{\circ}(\mathrm{cal} \mathrm{mol}$ |  |  |  |  |
| $\left.\mathrm{H} \mathrm{K}^{-1}\right)$ | - | - | $-60.01 /-52.81$ | $-60.54 /-59.04$ |
| HOMO | $-0.32 /-0.19$ | $-0.35 /-0.22$ | $-0.32 /-0.19$ | $-0.33 /-0.20$ |
| LUMO | $0.11 / 0.01$ | $-0.02 /-0.11$ | $-0.02 /-0.12$ | $-0.03 /-0.13$ |
| $\Delta \mathrm{E}(\mathrm{HOMO}-\mathrm{LUMO})$ | $-0.44 /-0.20$ | $-0.32 /-0.11$ | $-0.291 /-0.06$ | $-0.297 /-0.07$ |
| $\mu(\mathrm{eV})$ | $-0.10 /-0.09$ | $-0.1868 /-0.174$ | $-0.175 /-0.16$ | $-0.1862 /-0.171$ |
| $\mathrm{x}(\mathrm{eV})$ | $0.10 / 0.09$ | $0.1868 / 0.174$ | $0.175 / 0.16$ | $0.1862 / 0.171$ |
| $\eta(\mathrm{eV})$ | $0.22 / 0.10$ | $0.16 / 0.05$ | $0.145 / 0.032$ | $0.148 / 0.036$ |
| $\omega(\mathrm{eV})$ | $0.02 / 0.04$ | $0.106 / 0.27$ | $0.105 / 0.39$ | $0.11 / 0.40$ |


| Aqueous phase |  |  |  |  |
| :--- | :---: | :---: | :---: | :---: |
|  | $\beta$-CD free | AZ free | Orientation A | Orientation B |
| $\Delta \mathrm{H}^{\circ}\left(\mathrm{kcal} \mathrm{mol}^{-1}\right)$ | - | - | $-37.05 /-39.25$ | $-34.91 /-36.29$ |
| $\Delta \mathrm{G}^{\circ}\left(\mathrm{kcal} \mathrm{mol}^{-1}\right)$ | - | - | $-21.60 /-18.84$ | $-19.65 /-16.76$ |
| $\Delta \mathrm{~S}^{\circ}(\mathrm{cal} \mathrm{mol}$ |  |  |  |  |
| $\left.\mathrm{H} \mathrm{K}^{-1}\right)$ | - | - | $-51.64 /-66.23$ | $-50.95 /-65.52$ |
| HOMO | $-0.33 /-0.20$ | $-0.35 /-0.23$ | $-0.33 /-0.20$ | $-0.33 /-0.20$ |
| LUMO | $0.12 / 0.01$ | $-0.02 /-0.12$ | $-0.03 /-0.13$ | $-0.04 /-0.13$ |
| $\Delta(\mathrm{HOMO}-\mathrm{LUMO})$ | $-0.46 /-0.22$ | $-0.32 /-0.10$ | $-0.295 /-0.06$ | $-0.290 /-0.07$ |
| $\mu(\mathrm{eV})$ | $-0.10 /-0.09$ | $-0.19 /-0.180$ | $-0.182 /-0.168$ | $-0.188 /-0.171$ |
| $\mathrm{x}(\mathrm{eV})$ | $0.10 / 0.09$ | $0.19 / 0.180$ | $0.182 / 0.168$ | $0.188 / 0.171$ |
| $\eta(\mathrm{eV})$ | $0.23 / 0.11$ | $0.16 / 0.05$ | $0.147 / 0.033$ | $0.145 / 0.036$ |
| $\omega(\mathrm{eV})$ | $0.02 / 0.03$ | $0.111 / 0.29$ | $0.113 / 0.41$ | $0.12 / 0.43$ |

B ( $-37.85 \mathrm{kcal} \mathrm{mol}^{-1}$ ). The Frontier orbitals of $A Z / \beta-C D$ in the two obtained phases were calculated by B97D3/6$31 \mathrm{G}(\mathrm{d})$. Results indicate that HOMO orbit is localized on the host, and the LUMO orbit is localized on the guest molecule, which means mutual interactions are generated between $\beta$-CD and AZ (see Fig. 6).

## The Global Indices

The energy gap between HOMO and LUMO can be used in determining the global indices of the reactivity such as electronegativity $(\chi)$, electronic potential $(\mu)$, hardness $(\eta)$, and global electrophilicity index $(\omega)$. Indices of the reactivity were calculated by the methods WB97X-D/6-
$31 \mathrm{G}(\mathrm{d})$ and $\mathrm{B} 97 \mathrm{D} 3 / 6-31 \mathrm{G}(\mathrm{d})$ in gas and aqueous phases using the following equations:

$$
\begin{align*}
& \mu=\left(\mathrm{E}_{\text {Номо }}+\mathrm{E}_{\text {LUMO }}\right) / 2  \tag{6}\\
& \chi=-\mu=\left(\mathrm{E}_{\text {Номо }}+\mathrm{E}_{\text {LUMO }}\right) / 2  \tag{7}\\
& \eta=\left(\mathrm{E}_{\text {LUмо }}-\mathrm{E}_{\text {Номо }}\right) / 2  \tag{8}\\
& \omega=\mu^{2} / 2 \eta \tag{9}
\end{align*}
$$

Table 4 shows the global indices of reactivity. It is clear that the values of the electronic potential $(\mu)$ are negative in the


Fig. 6. The Frontier orbitals HOMO and LUMO of the $A Z / \beta-C D$ complex was obtained using the B97D3/6-31G(d) method in the gas phase.
two phases, and the two orientations. This demonstrates that the complexation of the $A Z$ in the $\beta-C D$ cavity is a spontaneous phenomenon. Using WB97X-D/6-31G(d) method in the gas and aqueous phases, the electronic chemical potential of the free AZ molecule was less than that of the free $\beta-C D$. This difference allows the charge transfer from the $\beta-C D$, with high electronic chemical potential ( $-0.10 /-0.10 \mathrm{eV}$ ), to AZ , with low electronic chemical potential ( $-0.18 /-019 \mathrm{eV}$ ) [36]. From the values in the Table 4, it is clear that the chemical hardness of $A Z / \beta-C D$ is important in both orientations, confirming the charge transfer. From the results obtained for the total global electrophilicity index, we can conclude that the compound is electrophilic.

## Atomic Charges

The charge distribution in the $A Z / \beta-C D$ complex was analyzed using two population analysis methods: The Mulliken Population Analysis (MPA), and NPA; our goal was to compare them and assess their utility. Mulliken
atomic charge analysis was performed to identify the partial atomic charges that o allow the qualitative understanding of the structures and reactivity of molecules. The charge distributions of atoms calculated by the NBO approach are presented in Table 5. WB97X-D/6-31G(d) and B97D3/6$31 \mathrm{G}(\mathrm{d})$ methods were used to study the free and encapsulated AZ in the gas phase and in different orientations. From these results, it can be seen that all the atomic charges of AZ were altered upon complexation with the host $\beta$-CD. The results showed that the positive charges were localized on hydrogen (H 171: 0.177/0.164) and sulfur atoms ( S 162: 1.361/1.285). The negative charges were localized on oxygen (O 160: -0.356/-0.331) and carbon atoms (C 170: -0.155/-0.128). Nitrogen atoms can be either positive ( N 158: $0.405 / 0.360$ ), due to the presence of high electronegative oxygen atoms ( O 159: -0.396/-0.368 and O 160: $-0.356 /-0.331$ ) in the adjacent position, or negative ( N 163: -0.577/-0.540), due to the attachment of the positively charged sulfur atom (S 162: 1.361/1.285). We can also see that in both orientations, the $H$ atoms (H 166,

Table 5. Variation of Mulliken Atomic Charges of AZ before and after Inclusion into $\beta$-CD Calculated by WB97X-D/6-31G(d) and B97D3/6-31G(d) in the Gas Phase

| $\mathrm{N}^{\circ}=$ Atome | AZ free | Orientation A | Orientation B |
| :---: | :---: | :---: | :---: |
| C 148 | -0.173/-0.142 | -0.174/-0.141 | -0.162/-0.130 |
| C 149 | -0.144/-0.111 | -0.144/-0.111 | -0.147/-0.126 |
| C 150 | -0.188/-0.172 | -0.138/-0.139 | -0.191/-0.189 |
| C 151 | -0.221/-0.194 | -0.193/-0.173 | -0.229/-0.205 |
| C 152 | 0.239/0.239 | 0.251/0.254 | 0.249/0.259 |
| C 153 | -0.154/-0.122 | -0.153/-0.122 | -0.166/-0.137 |
| H 154 | 0.200/0.164 | 0.199/0.165 | 0.203/0.169 |
| H 155 | 0.198/0.162 | 0.200/0.166 | 0.191/0.171 |
| H 156 | 0.234/0.203 | 0.221/0.208 | 0.236/0.219 |
| H 157 | 0.223/0.184 | 0.220/0.183 | 0.228/0.196 |
| N 158 | 0.396/0.352 | 0.405/0.360 | 0.414/0.365 |
| O 159 | -0.373/-0.344 | -0.396/-0.368 | -0.405/-0.379 |
| O 160 | -0.367/-0.340 | -0.356/-0.331 | -0.352/-0.330 |
| O 161 | -0.546/-0.508 | -0.564/-0.531 | -0.548/-0.512 |
| S 162 | 1.300/1.211 | 1.361/1.285 | 1.298/1.213 |
| N 163 | -0.514/-0.482 | -0.577/-0.540 | -0.524/-0.493 |
| O 164 | -0.512/-0.476 | -0.561/-0.530 | -0.513/-0.478 |
| C 165 | -0.225/-0.205 | -0.275/-0.270 | -0.250/-0.263 |
| H 166 | 0.212/0.187 | 0.233/0.211 | 0.224/0.230 |
| H 167 | 0.191/0.178 | 0.216/0.213 | 0.182/0.174 |
| C 168 | -0.001/0.009 | -0.029/-0.02 | -0.007/-0.013 |
| H 169 | 0.194/0.169 | 0.248/0.234 | 0.191/0.187 |
| C 170 | -0.145/-0.116 | -0.155/-0.128 | -0.129/-0.105 |
| H 171 | 0.145/0.135 | 0.177/0.164 | 0.153/0.145 |
| C 172 | -0.515/-0.478 | -0.521/-0.504 | -0.531/-0.536 |
| H 173 | 0.213/0.201 | 0.201/0.199 | 0.201/0.197 |
| H 174 | 0.160/0.143 | 0.162/0.145 | 0.191/0.184 |
| H 175 | 0.163/0.147 | 0.172/0.167 | 0.134/0.141 |
| C 176 | -0.494/-0.456 | -0.522/-0.505 | -0.513/-0.493 |
| H 177 | 0.166/0.152 | 0.175/0.170 | 0.149/0.135 |
| H 178 | 0.171/0.154 | 0.168/0.151 | 0.220/0.209 |
| H 179 | 0.168/0.152 | 0.173/0.174 | 0.154/0.151 |
| Charge transfer | 0.000/-0,004 | 0.036/0.056 | -0.049/-0.045 |

H 167, H 171, H 174) of AZ interact with the internal part of $\beta-C D$ increasing their atomic charges. A significant
change in trend was obtained in orientation A: C 168 (-0.001/0.009-0.029/-0.02). The data shows that the charge

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Table 6. Calculated Net Charges by Mulliken Population Method and Natural Population Analysis (NPA) of the AZ/ $\beta$-CD Complex by WB97X-D/6-31G(d) in the Gas Phase

|  | Orientation A |  | Orientation B |  |
| :--- | :---: | :---: | :---: | :---: |
| $\mathrm{N}^{\circ}=$ Atome | Mulliken charges | NPA | Mulliken charges | NPA |
| C 148 | -0.174 | -0.210 | -0.162 | -0.211 |
| C 149 | -0.144 | -0.212 | -0.147 | -0.218 |
| C 150 | -0.138 | -0.175 | -0.191 | -0.216 |
| C 151 | -0.193 | -0.307 | -0.229 | -0.329 |
| C 152 | 0.251 | 0.088 | 0.249 | 0.077 |
| C 153 | -0.153 | -0.223 | -0.166 | -0.218 |
| H 154 | 0.199 | 0.260 | 0.203 | 0.266 |
| H 155 | 0.200 | 0.261 | 0.191 | 0.255 |
| H 156 | 0.221 | 0.278 | 0.236 | 0.287 |
| H 157 | 0.220 | 0.275 | 0.228 | 0.281 |
| N 158 | 0.405 | 0.560 | 0.414 | 0.560 |
| O 159 | -0.396 | -0.405 | -0.405 | -0.417 |
| O 160 | -0.356 | -0.345 | -0.352 | -0.341 |
| O 161 | -0.564 | -0.978 | -0.548 | -0.973 |
| S 162 | 1.361 | 2.405 | 1.298 | 2.403 |
| N 163 | -0.577 | -0.761 | -0.524 | -0.735 |
| O 164 | -0.561 | -0.964 | -0.513 | -0.931 |
| C 165 | -0.275 | -0.268 | -0.250 | -0.261 |
| H 166 | 0.233 | 0.271 | 0.224 | 0.257 |
| H 167 | 0.216 | 0.240 | 0.182 | 0.226 |
| C 168 | -0.029 | -0.065 | -0.007 | -0.055 |
| H 169 | 0.248 | 0.283 | 0.191 | 0.251 |
| C 170 | -0.155 | -0.293 | -0.129 | -0.281 |
| H 171 | 0.177 | 0.260 | 0.153 | 0.249 |
| C 172 | -0.521 | -0.698 | -0.531 | -0.696 |
| H 173 | 0.201 | 0.251 | 0.201 | 0.253 |
| H 174 | 0.162 | 0.240 | 0.191 | 0.249 |
| H 175 | 0.172 | 0.233 | 0.134 | 0.207 |
| C 176 | -0.522 | -0.694 | -0.513 | -0.692 |
| H 177 | 0.175 | 0.234 | 0.149 | 0.223 |
| H 178 | 0.168 | 0.244 | 0.220 | 0.272 |
| H 179 | 0.173 | 0.236 | 0.154 | 0.228 |
|  |  |  |  |  |

transfer in the orientation $\mathrm{A}(0.036)$ is greater than in the orientation $B(-0.049)$, so the $A Z / \beta-C D$ complex is more stable in the orientation A than in the orientation B [37]. A method of natural population analysis has been developed to calculate atomic charges and orbital populations of molecular wave functions in general atomic orbital basis sets [38]. For the $A Z / \beta-C D$ complex, the net charges are
calculated by Natural Population Analysis (NPA). The calculated natural atomic charge values were obtained from the Natural Bond Orbital Analysis (NBO) [39] and are listed in Table 6. The natural population analysis is an alternative to conventional Mulliken population analysis, and seems to exhibit improved numerical stability to better describe the electron distributions in $A Z / \beta-C D$ complex.

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Table 7. Stabilization Energy $\mathrm{E}^{(2)}\left(\mathrm{kcal} \mathrm{mol}^{-1}\right)$ of the most Important Donor-acceptor Interactions Calculated by WB97X-D/6-31G(d) and B97D3/6-31G(d) in the Two Phases for the Two Orientations

| Orbital donor | Orbital acceptor | $\mathrm{E}^{(2)}\left(\mathrm{kcal} \mathrm{mol}^{-1}\right)$ <br> WB97X-D/B97D3 <br> Gas phase | $\mathrm{E}_{(2)}\left(\mathrm{kcal} \mathrm{mol}{ }^{-1}\right)$ <br> WB97X-D/B97D3 <br> Aqueous phase | d <br> $(\AA)$ |
| :--- | :--- | :---: | :---: | :---: |
| Orientation A |  |  |  |  |
| $\sigma(1)(\mathrm{O}$ 161-S 162) | $\sigma^{*}(1)($ C 63-H 134) | $0.61 / 0.47$ | $0.61 / 0.36$ | 2.34 |
| LP(2) (O 11) | $\sigma^{*}(1)($ C 165-H 166) | $3.76 / 2.37$ | $4.12 / 2.01$ | 2.30 |
| LP(1) (O 159) | $\sigma^{*}(1)($ O 44-H 117) | $3.01 / 1.48$ | $2.87 / 1.64$ | 2.19 |
| LP(2) (O 159) | $\sigma^{*}(1)($ O 33-H 107) | $12.06 / 10.62$ | $13.84 / 11.73$ | 1.87 |
| LP(1) (O 164) | $\sigma^{*}(1)($ O 44-H 117) | $4.89 / 3.43$ | $5.33 / 3.44$ | 2.02 |
| Total |  | $24.33 / 18.37$ | $26.77 / 19.18$ | - |
| Orientation B |  |  |  |  |
| LP(2) (O 16) | $\sigma^{*}(1)($ C 149-H 155) | $1.25 / 0.79$ | $1.17 / 0.81$ | 2.57 |
| LP(1) (O 62) | $\sigma^{*}(1)($ O 165-H 166) | $5.1 / 4.56$ | $4.81 / 2.7$ | 2.16 |
| LP(1) (O 159) | $\sigma^{*}(1)($ O 69-H 140) | $5.53 / 4.31$ | $5.98 / 4.09$ | 1.91 |
| LP(2) (O 159) | $\sigma^{*}(1)($ O 69-H 140) | $6.68 / 6.21$ | $6.41 / 4.64$ | 1.91 |
| Total |  | $18.56 / 15.87$ | $18.37 / 12.24$ | - |

## Natural Bond Orbital Analysis (NBO)

In order to determine intra- and intermolecular bounds and interactions [40] between guest AZ and host $\beta-\mathrm{CD}$, to identify, and quantify the different donor-acceptor interactions of the host/guest partners, we used the energy $\mathrm{E}^{(2)}$ in Eq. (10); if $\mathrm{E}^{(2)}$ is larger, the interactions between donors and acceptor is intense [41]. The delocalization of the electron density between occupied orbitals and unoccupied orbitals is related to the stabilizing donoracceptor interaction [42].

$$
\begin{equation*}
E^{(2)}=q_{i}{ }_{i}^{\frac{F(i, j)}{\varepsilon_{j}-\varepsilon_{i}}} \tag{10}
\end{equation*}
$$

Where $q_{i}$ is the donor orbital occupancy, $\varepsilon_{i}$ and $\varepsilon_{j}$ are diagonal elements, and $F_{i j}$ is the off diagonal NBO Fock matrix element. The donor-acceptor interactions and their corresponding $\mathrm{E}^{(2)}$ energies are shown in Table 7. As shown in Table 7, WB97X-D method gives the best values of $\mathrm{E}^{(2)}$. For orientation A , an interaction between the free doublet (LP) of donor orbital of the oxygen atom (O 159) of AZ and the anti-binding acceptor orbital $\sigma^{*}$ (O 33-H 107) of $\beta-\mathrm{CD}$ positioned at $1.87 \AA$ with a stabilization energy $\mathrm{E}^{(2)}$ of
$12.06 / 10.62 \mathrm{kcal} \mathrm{mol}^{-1}$ in the gas phase, another interaction is observed between the free doublet (LP) of donor orbital of oxygen atom ( O 164) and anti-binding acceptor orbital $\sigma *(\mathrm{O} 44-\mathrm{H} 117)$ positioned at $2.02 \AA$ with a stabilization energy $\mathrm{E}^{(2)}$ of $4.89 / 3.43 \mathrm{kcal} \mathrm{mol}^{-1}$. The same interaction was obtained between the free doublet (LP) of the donor orbital of oxygen atom ( O 159) and the anti-binding acceptor orbital $\sigma^{*}$ (O 69-H 140) that was positioned at $1.91 \AA$. In orientation B , lower energy value of $6.68 / 6.21 \mathrm{kcal} \mathrm{mol}^{-1}$ was obtained compared to orientation A. Orientation A is strongly stabilized by the formation of hydrogen. Intermolecular hydrogen bonds exist in the geometrical structures of both orientations (Fig. 7).

From the results of NBO calculations, we can confirm that the intermolecular hydrogen interactions and charge transfer between occupied and unoccupied orbitals of host/ guest have major contribution to the stabilization of the complex.

## ${ }^{1}$ H NMR Analysis

${ }^{1} \mathrm{H}$ NMR spectroscopy is one of the most useful techniques for studying host-guest systems, as it provides very interesting microscopic information about the structure


Fig. 7. Geometric structures of the tow orientations of the $A Z / \beta-C D$ complex optimized by the NBO method, WB97X-D/6-31G(d) $(a, b)$ in the gas phase.
of the formed molecule and the orientation of the embedded guest molecule. To better explore the introducing guest particles into the lumen of the host molecule, we calculated the chemical shifts $\delta$. In this part, variability in H NMR chemical transitions was studied using the Gauge-Including Atomic Orbital (GIAO) approach [43]. The B3LYP/6$31 \mathrm{G}(\mathrm{d})$ method was applied using single-point calculations on geometries optimized by WB97X-D/6-31G(d) and B97D3/6-31G(d). The method was found suitable for the theoretical Proton NMR spectroscopy of organic molecules $[44,45]$. NMR chemical shifts ( $\delta$ ) were calculated by subtracting the nuclear magnetic shielding tensors of protons in molecules of interest from those in tetramethyl silane (TMS) as a reference. Chemical shift ( $\delta$ ) was calculated by the equation:

$$
\begin{equation*}
\delta=\sigma T M S-\sigma \tag{11}
\end{equation*}
$$

Changes in the chemical shifts of the isolated AZ guests and their inclusion complexes are shown in Table 8 and Fig. 8.

The inclusion of $A Z$ in the $\beta-C D$ cavities was evidenced by the change in the chemical shifts of the last encapsulated protons with respect to the chemical shifts of the same protons in the free form. The values of the calculated and


Fig. 8. Chemical shifts experimental [10] and calculated of free $A Z$ protons and inclusion complexes $A Z / \beta-C D$ by the GIAO approach, B3LYP/6-31G(d).
experimental chemical shifts [10] (H 166: 2.80 ppm ), before and after the complexation, are close in orientation A (H 166: 3.42 ppm ). The difference in most values does not exceed 1 ppm from orientation B ( $\delta \mathrm{H}$ 166: 4.55 ppm ). The largest difference between theoretical chemical transformations and experimental chemical transformations in proton (H 156: 9.04 ppm ) was observed for direction B. It should be noted that the two theoretical structures presenting minimum energy are in both orientations, but on

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Table 8. ${ }^{1} \mathrm{H}$ NMR Chemical Shifts (ppm) of AZ before and after Complexation Calculated by GIAO Method at B3LYP/6-31G(d) Optimized with WB97X-D/6-31g(d) and B97D3/6-31G(d) in the Aqueous Phase

|  |  | Calculated |  | Experimental |  |
| :--- | :---: | :---: | :---: | :---: | :---: |
| Protons | AZ free | AZ in complex <br> Orientation A | AZ incomplexe <br> Orientation B | AZ free | AZ in complex |
| $\mathrm{H}(157)$ | $8.04 / 0.85$ | $8.07 / 8.20$ | $8.50 / 8.71$ | 8.52 | 8.17 |
| $\mathrm{H}(154)$ | $7.99 / 8.18$ | $8.08 / 8.24$ | $8.58 / 8.72$ | 8.14 | 7.71 |
| $\mathrm{H}(155)$ | $7.99 / 8.17$ | $8.13 / 8.28$ | $8.49 / 8.75$ | 8.02 | 7.90 |
| $\mathrm{H}(156)$ | $8.42 / 8.54$ | $8.48 / 8.50$ | $9.04 / 8.87$ | 7.68 | 8.50 |
| $\mathrm{H}(166)$ | $2.93 / 3.10$ | $3.42 / 3.18$ | $4.55 / 4.41$ | 1.50 | 2.80 |
| $\mathrm{H}(167)$ | $2.50 / 2.61$ | $2.70 / 2.86$ | $2.40 / 2.60$ | 1.50 | 2.38 |
| $\mathrm{H}(169)$ | $2.46 / 2.58$ | $3.95 / 3.94$ | $2.99 / 2.86$ | 1.59 | 2.75 |
| $\mathrm{H}(171)$ | $1.47 / 1.70$ | $2.50 / 2.66$ | $1.74 / 1.77$ | 1,98 | 1.87 |
| $\mathrm{H}(173)$ | $2.38 / 2.47$ | $1.98 / 2.24$ | $2.44 / 2.56$ | 0.88 | 0.82 |
| $\mathrm{H}(174)$ | $1.05 / 1.21$ | $1.36 / 1.56$ | $2.15 / 2.04$ | 0.88 | 0.82 |
| $\mathrm{H}(175)$ | $0.90 / 1.05$ | $1.57 / 1.48$ | $1.19 / 1.30$ | 0.88 | 0.82 |
| $\mathrm{H}(177)$ | $0.78 / 0.94$ | $1.51 / 1.45$ | $0.74 / 1.00$ | 0.84 | 0.82 |
| $\mathrm{H}(178)$ | $0.92 / 1.08$ | $1.36 / 1.56$ | $2.21 / 1.98$ | 0.84 | 0.82 |
| $\mathrm{H}(179)$ | $0.85 / 0.98$ | $1.80 / 1.79$ | $0.96 / 1.11$ | 0.84 | 0.82 |

the basis of our theoretical results, the orientation A can be considered as the most convenient structure.

## Non-covalent Interaction Analysis (NCI)

The non-covalent interaction analysis method provides a graphic visualization of regions in which non-covalent interactions such as hydrogen bonds, van der Waals interactions, and repulsive steric interactions [46,47] produce in real space. Recently, the NCI analysis has been used to identify the weak interactions from the AIM analysis $[48,49]$. In the 3D spatial visualization of NCI isosurface shown in Fig. 9, the color-coding scheme is as follows: Van der Waals interactions are indicated by a green spot, strong hydrogen bond interactions are represented by a blue spot, and the repulsive steric forces are visualized by the red spot. From the NCI isosurface (Fig. 9), we observed green spots between $A Z$ and $\beta-C D$ in the orientations $A$ and $B$, indicating weak attraction due to the van der Waals interaction. We also observed some blue spots for hydrogen bond interactions between guest and host. There was also
the appearance of weak van der Waals, and weak intramolecular hydrogen bond interactions in $\beta-\mathrm{CD}$, between the primary and secondary hydroxyls, and steric repulsions in the aromatic rings of $A Z$ and $\beta-C D$.

## CONCLUSIONS

This theoretical work explored the detailed study of the inclusion complex of $A Z / \beta-C D$. The DFT functionals B3LYP, WB97X-D, and B97D3, and 6-31G(d) basis set were used in both gas and aqueous phases. Orientation A was more preferable than orientation $B$ in both the gas and aqueous phases, which is in good agreement with the experimental results. The best results were obtained using WB97X-D and B97D3/6-31G(d). Geometry optimization calculations for the complex in the aqueous phase were almost similar to those in the gas phase. The analysis of the thermodynamic calculations indicated the negative valued for $\Delta G, \Delta H$, and $\Delta S$, suggesting that the formation of $A Z / \beta$ CD inclusion complexes in vacuo is a spontaneous and


Fig. 9. NCI isosurfaces for the $A Z / \beta-C D$ inclusion complex calculated by method WB97X-D/6-31G(d) in gas phase.
enthalpy-driven process. The charge distribution calculated using NBO method indicated that when the guest molecule interacts with $\beta-C D$, its charge distribution changes. The NBO and NCI analysis showed that the driving forces for the formation of complexes were formation of intermolecular hydrogen bonds. Finally, the results of the RMN and GIAO calculations were in agreement with experiment.

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